

Laser polishing - numerical modelling using a mesh-free incompressible



EPSRC Centre for
Innovative Manufacturing in
**LASER-BASED
PRODUCTION
PROCESSES**

SPH method

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Introduction

- The laser polishing process leads to local melting (50-100 μ m) of surface and subsequent re-solidification in a smoother state.
- A feasibility study is pursued in order to model the laser polishing of stainless steel using Smoothed Particle Hydrodynamics; a novel mesh-less numerical method will enable deeper analysis of phenomena and inexpensive virtual testing.
- Incorporating a wide range of physical phenomena including surface tension, Marangoni forces, thermal conduction; phase change and latent heat.

Motivation

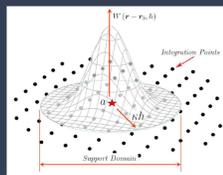
- Experimental prototyping aims to improve final surface quality of additively manufactured (AM) structures.
- The laser polishing process is based on melting and subsequent solidification of a micro-layer of material, using a scanning laser beam as the heat source for a smooth topography may be expensive in material acquisition, processing time and rapid measurement ability.
- A mature, efficient and accurate multi-physics code is desirable to interpret experimental results, reveal novel physical mechanisms and save on mentioned costs.

SPH-Methodology

- Lagrangian particle method using a kernel and its derivatives to discretise continuum equations. Particle nature renders re-meshing unnecessary; high distortion not penalised.
- Standard weakly compressible SPH (WCSPH) based on sound speed with Pressure-density equation of state; small time-steps required, noisy pressure possible.
- Tensile/compressive instability requires corrective terms.
- Kd-tree nearest neighbour algorithm implemented.

ISPH

Multi-dimensional kd-tree



kernel and support range.

- Incompressible SPH (ISPH) with Pressure-Poisson equation solver. Implemented for density invariant flows.
- Faster and more accurate than WCSPH though higher memory overhead required.

Numeric Framework

Heat Boundary Conditions and material Model:

- (Distant) Thermal boundary condition enabled contracting of problem domain
- Internal energy, latent heat and melting
- Laser profile: Gaussian external source
- exponential decay into substrate

$$h = \begin{cases} c_s T & \text{solid: } T < T_s \\ c_s T_s + c_{in}(T - T_s) & \text{part-melt: } T_s \leq T \leq T_l \\ c_s T_s + c_{in}(T_l - T_s) + c_l(T - T_l) & \text{liquid: } T > T_l \end{cases}$$

$$\dot{h} = c_v \dot{T}$$

$$T_i = T_b + x_{ib} \frac{\Delta T_{ib}}{\Delta x_{ib}}$$

Fluid Model:

- Full Navier-Stokes equations
- Continuum Surface Force (CSF) macroscopic model formulated for single phases
- Corrective-SPH (CSPH) gradients for free surfaces.

$$\nabla \mathbf{U}^* = \nabla \left(\frac{\nabla P}{\rho} \right) \Delta t$$

$$\rho \ddot{x}_i = -\nabla P + \mu \nabla^2 \mathbf{U} + \delta_c \gamma \kappa \hat{\mathbf{n}} + \nabla \gamma \cdot \hat{\mathbf{t}} + \mathbf{F}_b$$

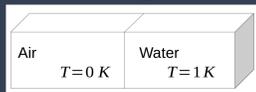
Thermal effects

Discontinuous thermal conduction rod test

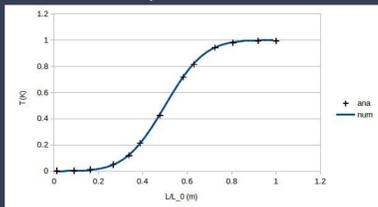
Full and free surface modelling of thermal conduction, validated against analytic (erf) function for a cooling bar:

- Continuous bar
- Discontinuous bar with ratios: $\rho=1000:1.2$, $\kappa=0.62:0.0254$, $c=4.19:1.01$

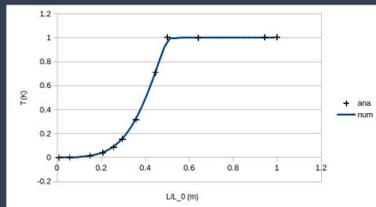
Numeric errors peak at 2.1%



Numeric setup:



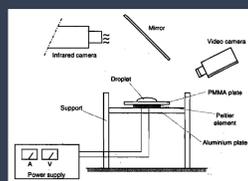
Continuous materials t=10s.



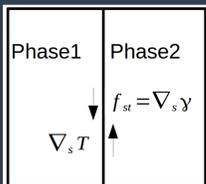
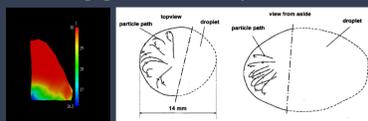
Discontinuous materials t=10s.

Marangoni Discretisation

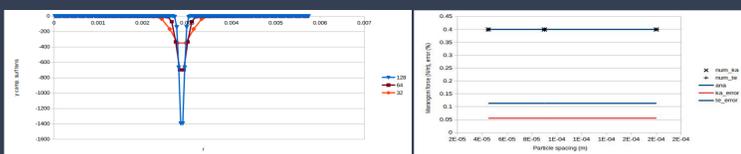
- Component of surface tension normal to the surface arises through gradients of surface tension caused by chemical (e.g. soapy water, coffee stains) or thermal (e.g. thermo-capillary convection) anisotropy.
- Marangoni force validated for interface, normal to thermal gradient
- Force Convergence Test performed along interface for both curvature and stress divergence surface tension methods. Results show good agreement between analytic and numeric quantities.



Thermocapillary droplet experiment [1] and subsequent motion



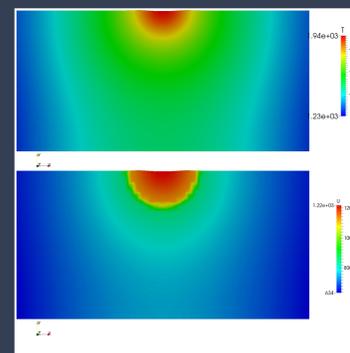
Numeric setup:



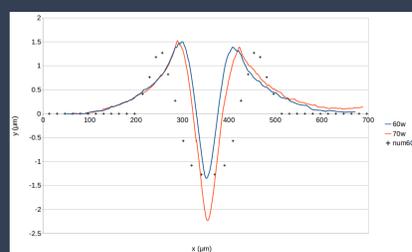
Convergence test for 32², 64², 128² particle grids

Spot beam melting/re-solidification Stainless steel power/duration variance test

Spot beam for a varying beam duration and power SPI fibre laser



Temperature and Internal energy in the melt zone.



Surface profile post-solidification

Laser properties:

Beam radius: 40 μ m, angle 90 $^\circ$

Material properties:

Dimensions: 500x500x300mm,

Density: 8000kgm⁻³,

Surface tension (air): 1.9Nm⁻¹

Kinematic viscosity: 0.75 μ m²s⁻¹

Thermal conductivity: 16.3Wm⁻¹K⁻¹,

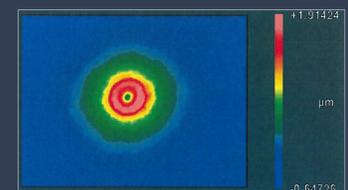
Thermal absorptivity: 0.3

Specific heat fluid: 712 Jkg⁻¹K⁻¹

Marangoni temp factor: -3.4e-4Nm⁻¹K⁻¹

Latent heat: 247 kJkg⁻¹

Liquidus, solidus temperature: 1697, 1727K



Experimental xy-data [2] (40W, 2.5ms).

Spot beam test varying laser duration and power.

- Power tests: 40, 50, 60, 70, 80, 90, 100W for 2ms
- Duration tests: 2.5, 5, 7.5, 10, 12.5, 15, 17.5, 20ms at 40W

Further developments

- 2d/3d beam spot tests ongoing.
- Different materials to include Cobalt-Chrome (CoCr), Titanium alloy (Ti6Al4V) testing
- Beam scanning tests to include scan angle and pattern variance.
- Material stress/thermal softening inclusion predicted to alleviate edge anomalies in beam spot tests.

Conclusions

- Numerical results show strong correlation to experimental post lasing surface scans.
- ISPH satisfies need for an efficient and effective modelling algorithm, capable of modelling the full set of physics required to simulate surface melts.

[1]. den Boer, A. W. J. P. (1996). Marangoni convection: numerical model and experiments. Eindhoven University of Technology.

[2]. Courtesy of Wojciech S. Gora, W.S.Gora@hw.ac.uk

Acknowledgements

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